



FACULTY OF ENGINEERING
END OF SEMESTER EXAMINATIONS - APRIL 2025

PROGRAMME: BACHELOR OF ELECTRICAL AND CONTROL ENGINEERING

YEAR/SEM: YEAR 3/SEMESTER 2

COURSE CODE: ELE3212

NAME: CONTROL SYSTEMS I

DATE: 2025-04-17

TIME: 2:00-5:00PM

INSTRUCTIONS TO CANDIDATES:

1. Read the instructions very carefully
2. The time allowed for this examination is STRICTLY three hours
3. Read each question carefully before you attempt and allocate your time equally between all the Sections
4. Write clearly and legibly. Illegible handwriting cannot be marked
5. Number the questions you have attempted
6. Use of appropriate workplace examples to illustrate your answers will earn you bonus marks
7. Any examination malpractice detected will lead to automatic disqualification.

DO NOT WRITE ANYTHING ON THE QUESTION PAPER

Section A CHOOSE ANY TWO QUESTIONS FROM THIS SECTION

Question 1:

Total: 25 Marks

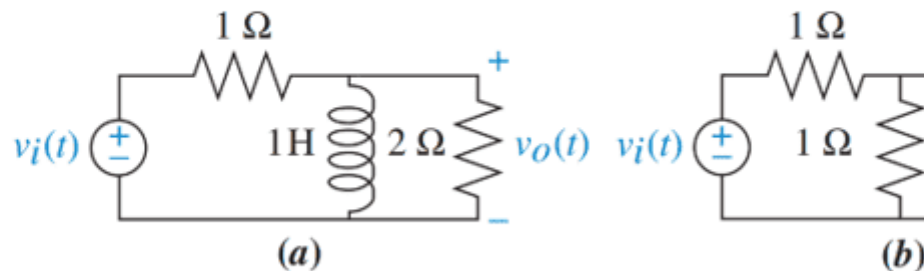
For the transfer function shown below, find the locations of the poles and **Marks]**, and then write an expression for the general form of the step response inverse Laplace transform **[15 Marks]**. State the nature of each response (underdamped, and so on).

$$T(s) = \frac{5}{(s + 3)(s + 6)}$$

Question 2:

Total: 25 Marks

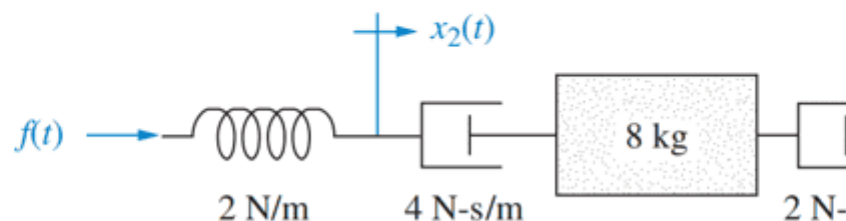
Find the transfer function, $G(s) = V_o(s)/V_i(s)$, for each network **(a) [12**



Question 3:

Total: 25 Marks

Find the transfer function, $G(s) = X_2(s)/F(s)$, for the translational mechanical system (Hint: place a zero mass at $x_2(t)$.)



Question 4:

Total: 25 Marks

- 1) Name the performance specification for first-order systems. **[2 Marks]**
- 2) What does the performance specification for a first-order system mean? **[2 Marks]**
- 3) In a system with an input and an output, what poles generate the oscillation? **[2 Marks]**
- 4) In a system with an input and an output, what poles generate the steady-state error? **[2 Marks]**
- 5) The imaginary part of a pole generates what part of a response? **[2 Marks]**
- 6) The real part of a pole generates what part of a response? **[2 Marks]**
- 7) What is the difference between the natural frequency and the damped natural frequency? **[4 Marks]**
- 8) If a pole is moved with a constant imaginary part, what will the response be? **[2 Marks]**
- 9) If a pole is moved with a constant real part, what will the response be? **[2 Marks]**
- 10) What pole locations characterize (a) the underdamped system, (b) the overdamped system, and (c) the critically damped system? **[3 Marks]**
- 11) Name two conditions under which the response generated by a pole is oscillatory. **[2 Marks]**

Section B CHOOSE ANY TWO QUESTIONS FROM THIS SECTION

Question 1:

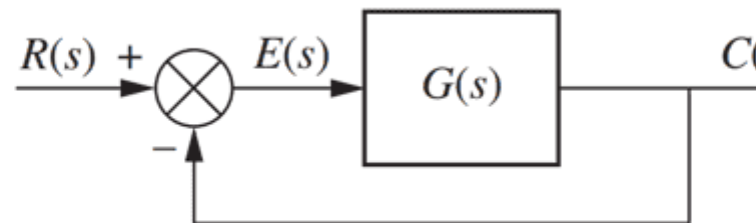
Total: 25 Marks

- 1) Name two sources of steady-state errors. **[2 Marks]**
- 2) A position control, tracking with a constant difference in velocity, has a steady-state position error in the steady state? **[4 Marks]**
- 3) Name the test inputs used to evaluate steady-state error. **[3 Marks]**
- 4) How many integrations in the forward path are required in order to eliminate steady-state error for each of the test inputs listed in 3) above? **[4 Marks]**
- 5) Increasing system gain has what effect upon the steady-state error? **[2 Marks]**
- 6) For a step input, the steady-state error is approximately the reciprocal of the static error constant if what condition holds true? **[2 Marks]**
- 7) What is the exact relationship between the static error constant and the steady-state errors for ramp and parabolic inputs? **[4 Marks]**
- 8) What information is contained in the specification $K_p = 10000$? **[2 Marks]**

Question 2:

Total: 25 Marks

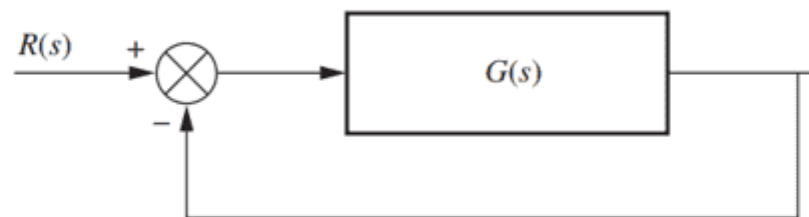
For the unity feedback system shown in the figure below, where $G(s)$ is the transfer function, calculate the steady-state errors for the following test inputs: $25u(t)$; $37tu(t)$; $47t^2u(t)$.



Question 3:

Total: 25 Marks

Sketch the root locus for the unity feedback system shown in the figure below, where $G(s)$ is the transfer function, for the following functions:



a) $G(s) = \frac{K(s+2)(s+6)}{s^2+8s+25}$

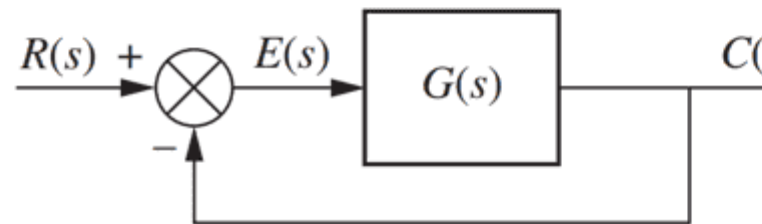
b) $G(s) = \frac{K}{(s+1)^3(s+4)}$

Question 4:

Total: 25 Marks

For the unity feedback system shown in the figure below, where $G(s) =$

$$\text{Given } \%OS = e^{-\left(\frac{\zeta\pi}{\sqrt{1-\zeta^2}}\right)} \times 100 ; T_s = \frac{4}{\zeta\omega_n}$$



- what is the expected percent overshoot for a unit step input? **[5 Marks]**
- What is the settling time for a unit step input? **[5 Marks]**
- What is the steady-state error for an input of $5u(t)$? **[5 Marks]**
- What is the steady-state error for an input of $5tu(t)$? **[5 Marks]**
- What is the steady-state error for an input of $5t^2u(t)$? **[5 Marks]**